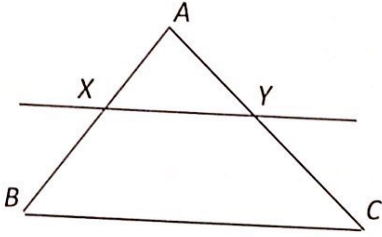


Q6	Model Solution – 25 Marks	Marking Notes
(a)	<p><i>Diagram:</i></p>  <p><i>Given:</i> A triangle <math>ABC</math> and a line <math>XY</math> parallel to <math>BC</math> which cuts <math>AB</math> in the ratio <math>s : t</math> where <math>s, t \in \mathbb{N}</math>.</p> <p><i>To Prove:</i> <math>[AY] : [YC] = s : t</math></p> <p><i>Construction:</i> Divide <math>[AB]</math> into <math>s + t</math> equal parts, <math>s</math> of them lying along <math>[AX]</math> and <math>t</math> of them lying along <math>[XB]</math>. Through each point of division draw a line parallel to <math>[BC]</math></p> <p><i>Proof:</i> By a previous theorem the parallel lines cut off segments of equal length along <math>[AC]</math>. Therefore <math>[AC]</math> is divided into <math>s + t</math> equal parts with <math>s</math> of them forming <math>[AY]</math> and <math>t</math> of them forming <math>[YC]</math>. Let <math>k</math> be the length of one segment on <math>[AC]</math>. <math>[AY] : [YC] = ks : kt = s : t</math></p>	<p><b>Scale 15D (0, 4, 7, 11, 15)</b></p> <p><i>Low Partial Credit:</i> Relevant diagram drawn</p> <p><i>Mid Partial Credit:</i> Construction clearly indicated</p> <p><i>High Partial Credit:</i> Proof missing 1 relevant step</p>

(b)

$$|XY| = \sqrt{4^2 + 3^2} = 5$$

$$|ZC| = 5$$

$$|BZ| = 10\text{cm}$$

Or

$$\frac{8}{4} \text{ or } \frac{2}{1} = \frac{|BZ|}{5} \rightarrow |BZ| = 10\text{cm}$$

Or

$$\frac{4}{12} = \frac{5}{5 + |BZ|}$$

$$4|BZ| + 20 = 60 \rightarrow |BZ| = 10\text{ cm}$$

Similarly:  $\frac{3}{9} = \frac{5}{5 + |BZ|}$

**Scale 10C (0, 3, 7, 10)**

*Low Partial Credit:*

|XY| or |BX| or |CY| found

Pythagoras with some substitution

*High Partial Credit:*

|ZC| or |BC| found

Ratios formulated with |BZ| the sole unknown